

Charge Radius Measurement of ${}^6\text{He}$ in an Atom Trap

Peter Mueller

Argonne National Laboratory

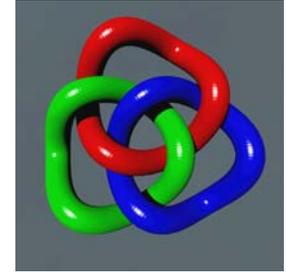


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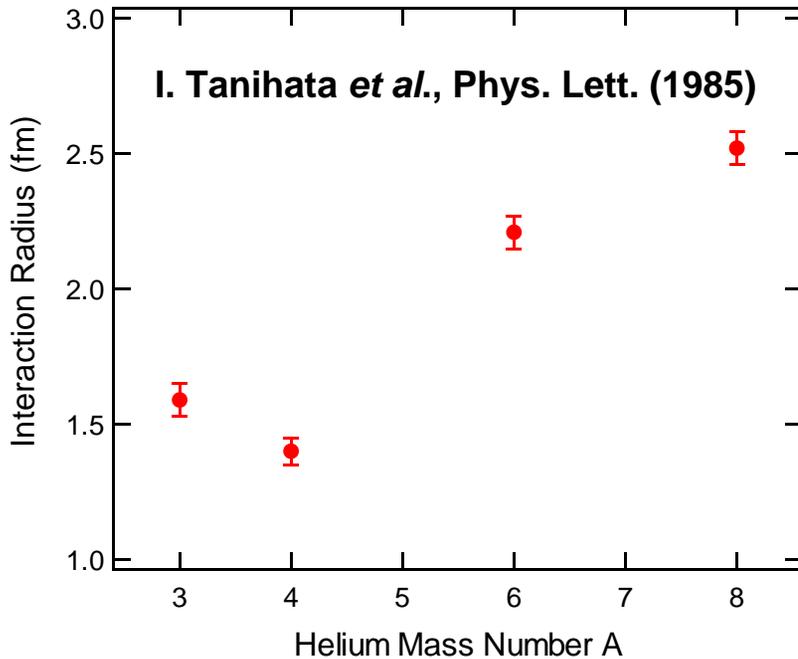


Neutron Halo Nuclei ${}^6\text{He}$ and ${}^8\text{He}$

Isotope	Half-life	Spin	Isospin	Core + Valence
He-6	807 ms	0^+	1	$\alpha + 2n$
He-8	119 ms	0^+	2	$\alpha + 4n$



Borromean



Core-Halo Structure

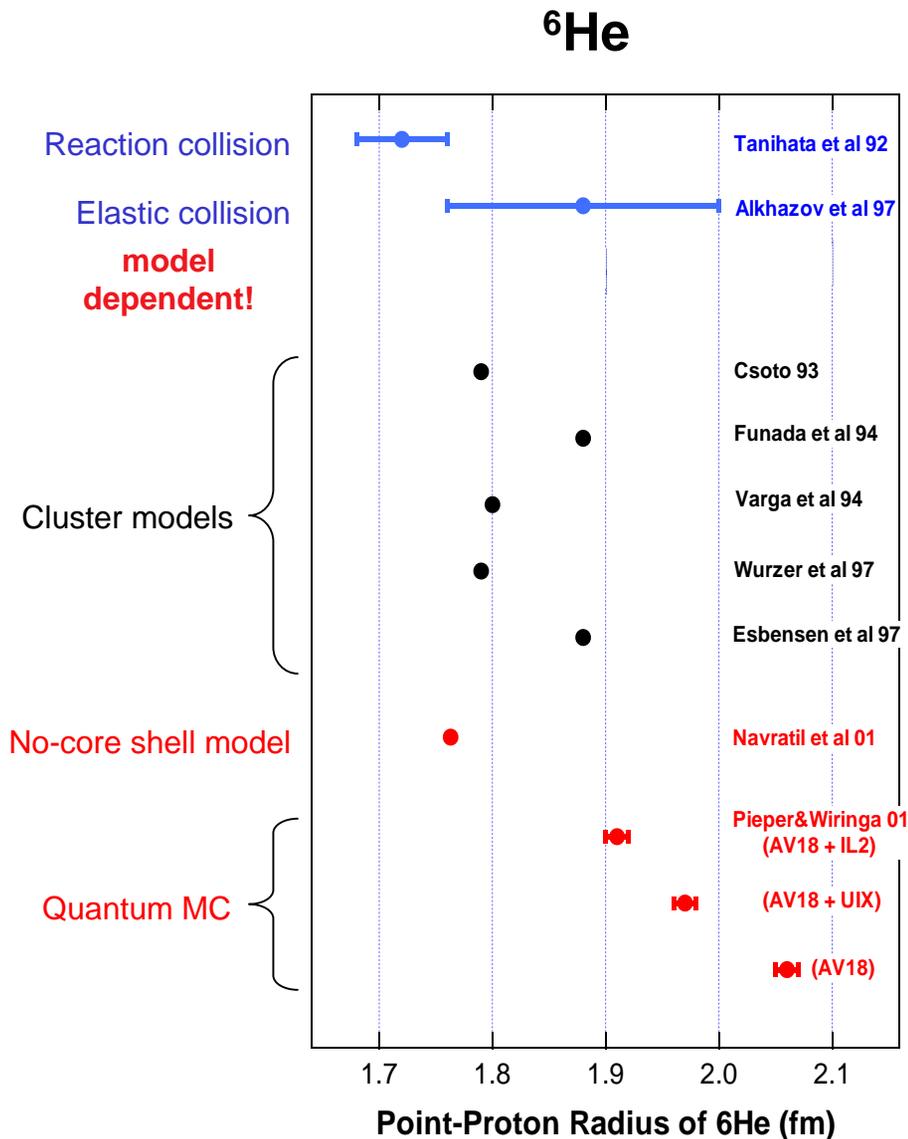
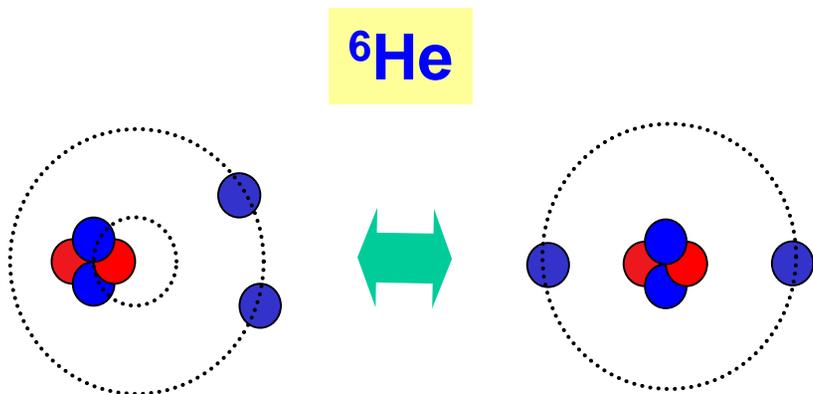
$$\sigma_I(6\text{He}) - \sigma_I(4\text{He}) = \sigma_{-2n}(6\text{He})$$

I. Tanihata *et al.*, Phys. Lett. (1992)

Charge Radii of He Isotopes

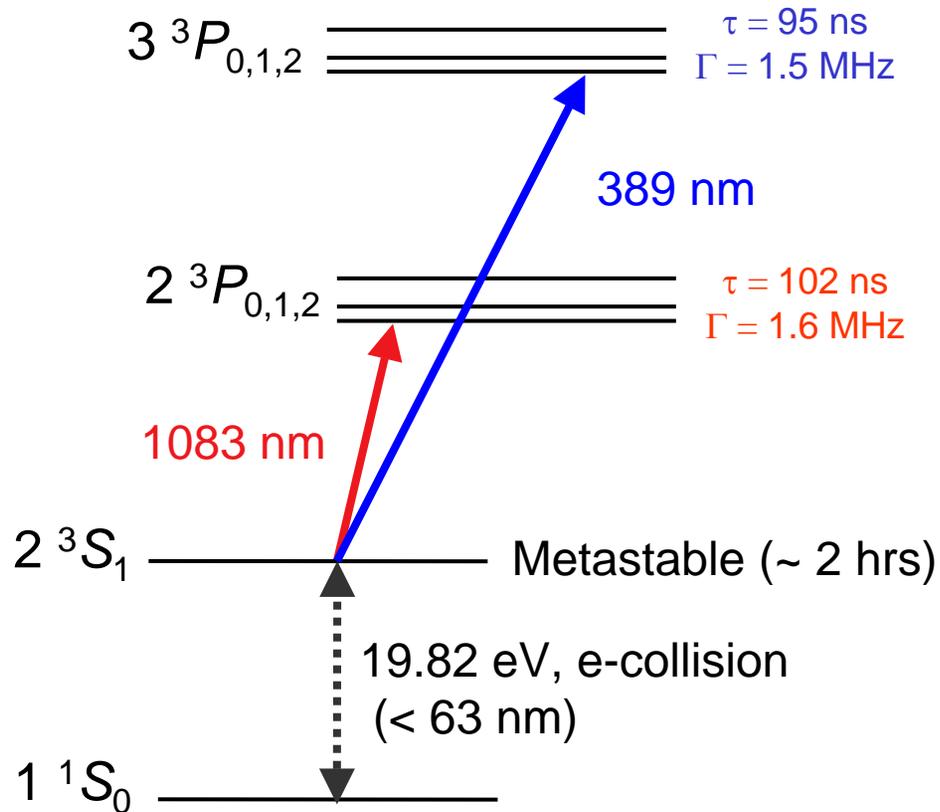
RMS point proton radii (fm):
theory and **experiment**

	He-3	He-4	He-6	He-8
QMC Theory	1.74(1)	1.45(1)	1.91(1)	1.88(1)
μ -He Lamb Shift		1.474(7)		
Atomic Isotope Shift	1.766(6)		?	?
p-He Scattering			1.95(10) _{GG} 1.81(09) _{GO}	1.68(7) _{GG} 1.42(7) _{GO}

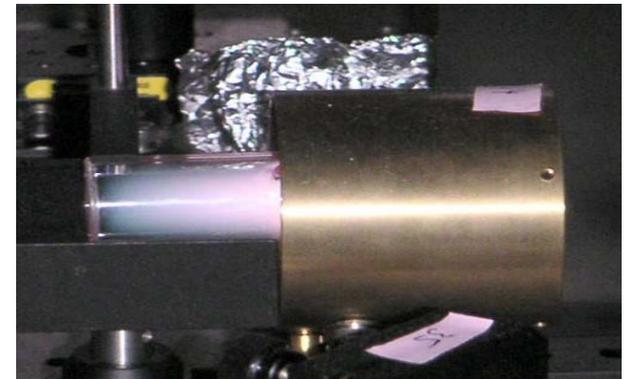


Atomic Energy Levels of Helium

He energy level diagram



He discharge

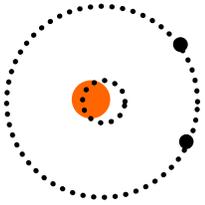


Atomic Isotope Shift

$$\text{Isotope Shift} \quad \delta\nu = \delta\nu_{\text{MS}} + \delta\nu_{\text{FS}}$$

Mass shift:

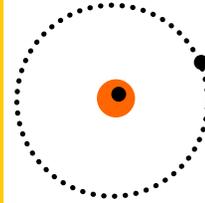
due to nucleus recoil



$$\delta\nu_{\text{MS}} \propto \frac{A - A'}{AA'}$$

Field shift:

due to nucleus size



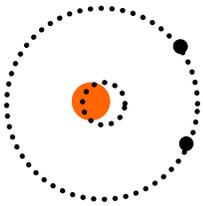
$$\delta\nu_{\text{FS}} \propto Z \times \Delta[\Psi(0)]^2 \times \delta\langle r^2 \rangle$$

Atomic Isotope Shift

$$\text{Isotope Shift} \quad \delta\nu = \delta\nu_{\text{MS}} + \delta\nu_{\text{FS}}$$

Mass shift:

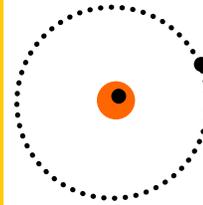
due to nucleus recoil



$$\delta\nu_{\text{MS}} \propto \frac{A - A'}{AA'}$$

Field shift:

due to nucleus size



$$\delta\nu_{\text{FS}} \propto Z \times \Delta[\Psi(0)]^2 \times \delta\langle r^2 \rangle$$

$$\text{IS}(2^3\text{S}_1 - 3^3\text{P}_2) = 43196.202(16) + 1.008(\langle r^2 \rangle_{\text{He4}} - \langle r^2 \rangle_{\text{He6}}) \text{ MHz}$$

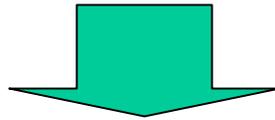
*G.W.F. Drake, Univ. of Windsor, *Nucl. Phys. A737c*, 25 (2004)

100 kHz error in frequency \leftrightarrow 1% error in radius

Spectroscopy of ^6He

Technical challenges:

- Short lifetime, small sample
- Metastable efficiency $\sim 10^{-5}$
- Precision requirement (IS ~ 40 GHz, Field shift ~ 1 MHz)



Solution:

Laser spectroscopy of **individual trapped $^6\text{He}^*$** atoms

- ✓ **High resolution:** cold atoms, Doppler width largely reduced
- ✓ **High sensitivity:** capable of detecting a single atom

Approach & Collaboration

Production



Trap and Detection



Precision Spectroscopy



Subtract Mass Shift by
Atomic Theory



Compare Results with
Nuclear Theory

Collaboration list

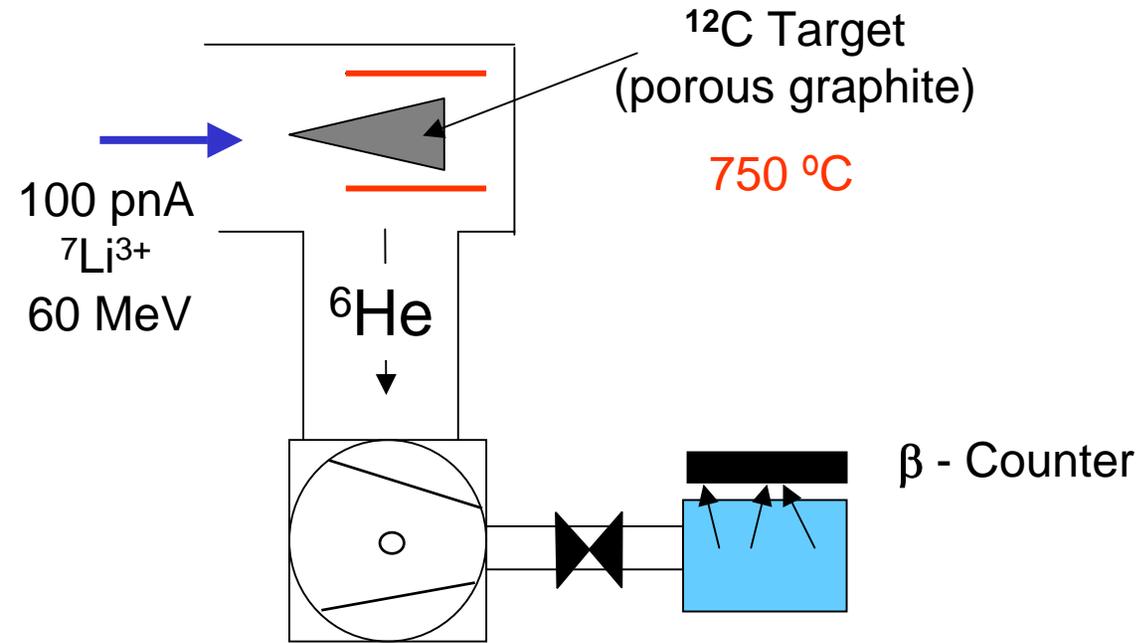
ATTA: P. Mueller, L.-B. Wang*, K. Bailey,
R.J. Holt, Z.-T. Lu, T. O'Conner
Physics Division, Argonne National Laboratory
**University of Illinois at Urbana-Champaign*

Heavy Ion Group: J.P. Greene, D. Henderson,
R. Janssens, C.L. Jiang, R.C. Pardo,
K.E. Rehm, J.P. Schiffer, X.D. Tang
Physics Division, Argonne National Laboratory

Atomic Theory: G.W.F. Drake
University of Windsor, Canada

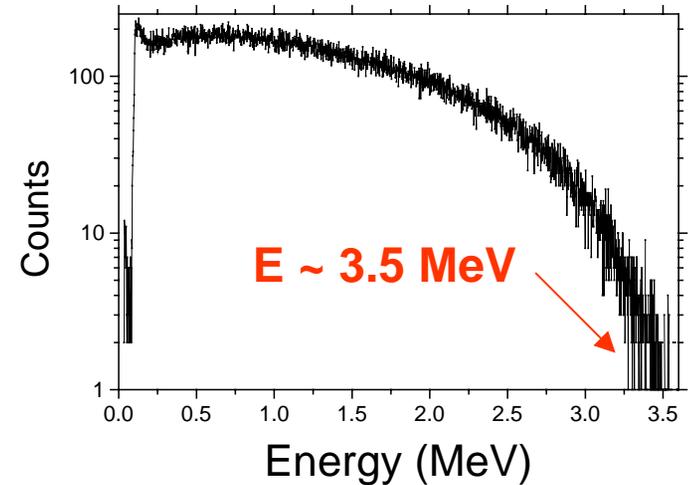
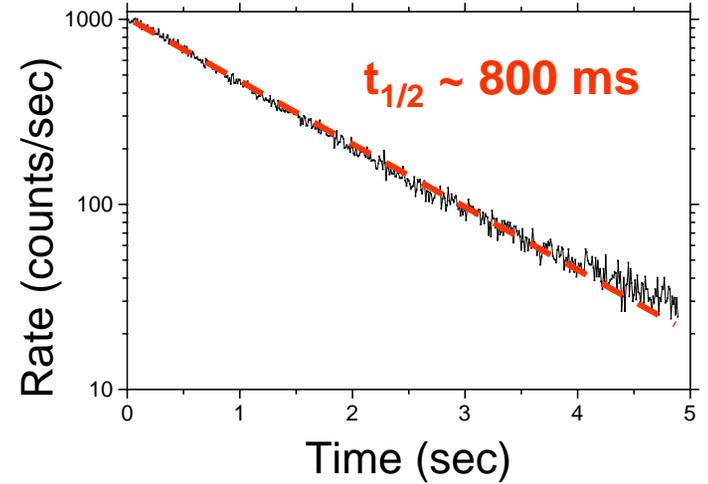
${}^6\text{He}$ - Production at ATLAS

${}^{12}\text{C}({}^7\text{Li}, {}^6\text{He}){}^{13}\text{N}$ - Reaction

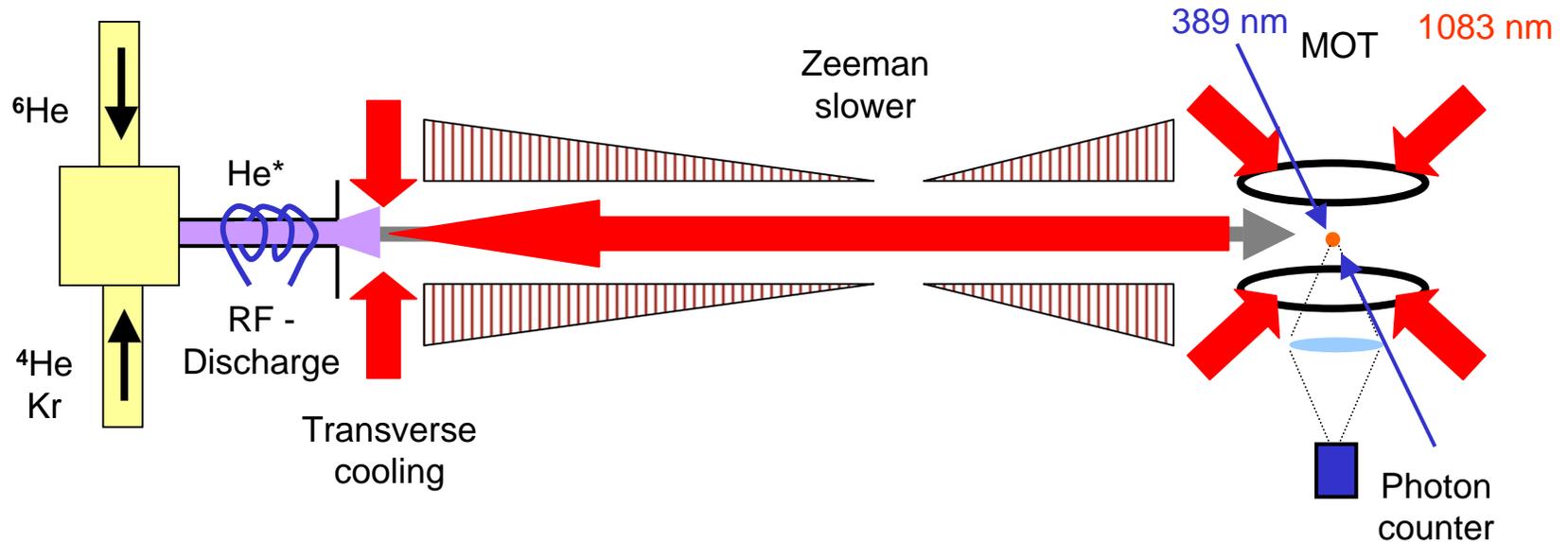
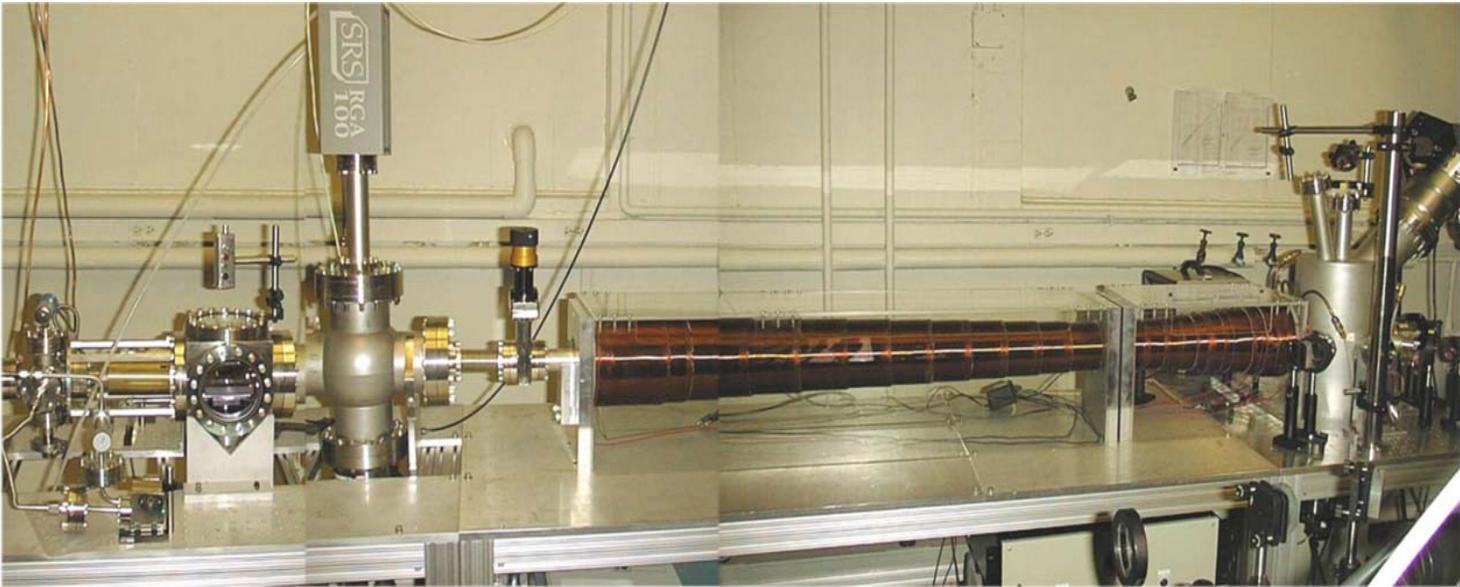


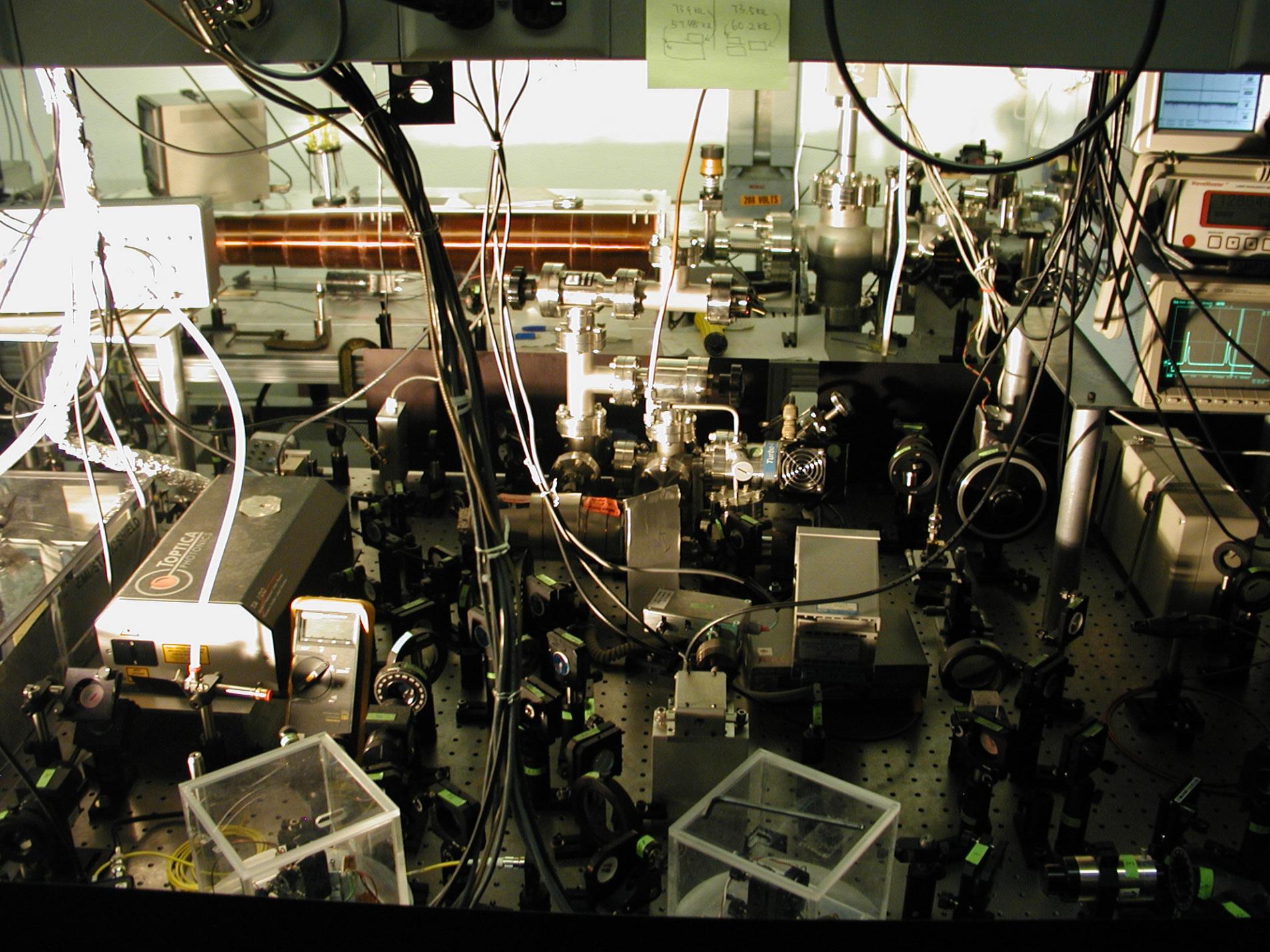
 ${}^6\text{He}$ atoms extracted: $\sim 1 \times 10^6/\text{s}$

Identification of ${}^6\text{He}$

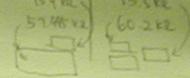


Atom Trapping of Helium



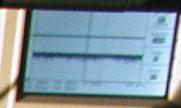


73.9 Hz 73.5 Hz
57.98 Hz 60.2 Hz

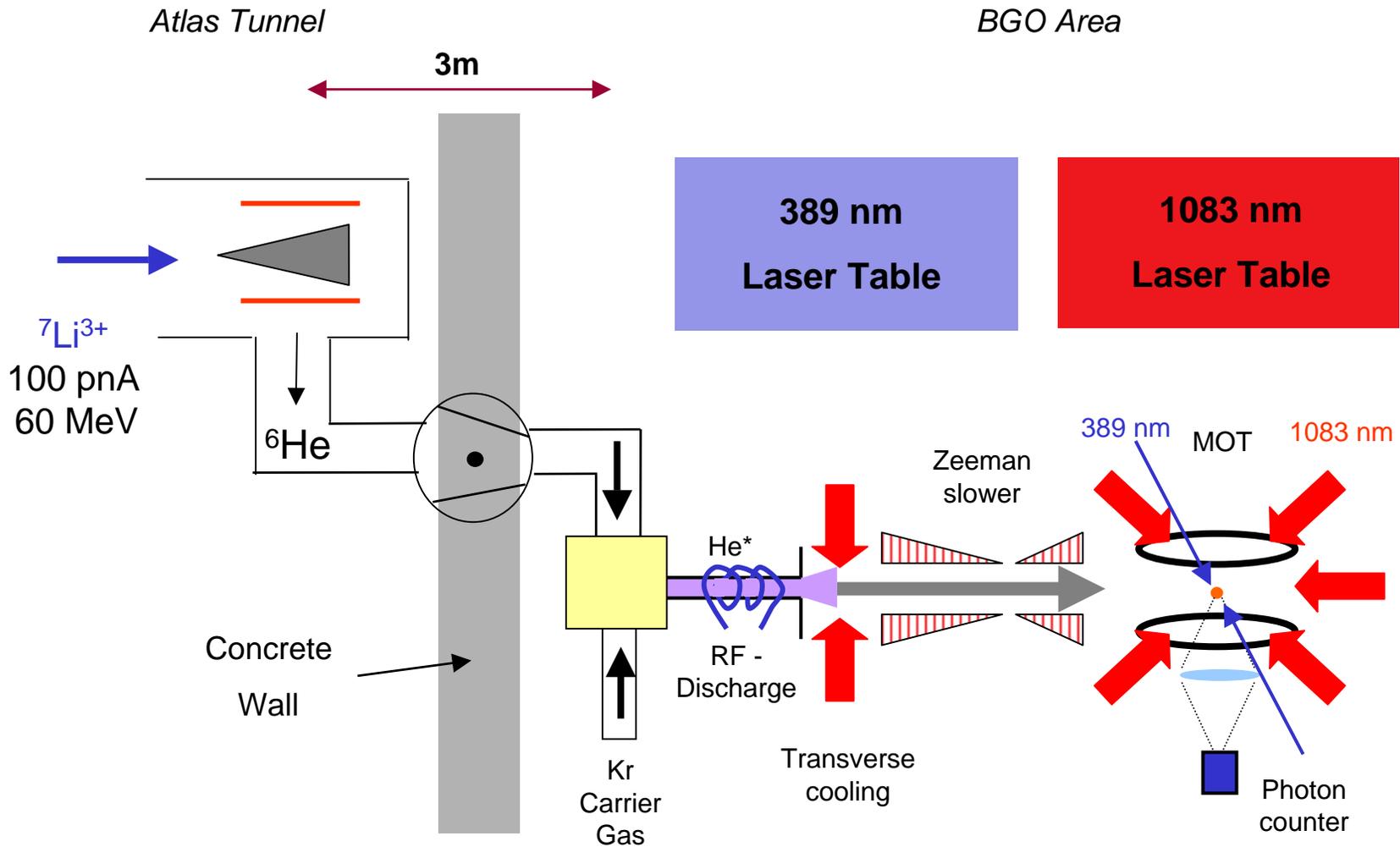


200 VOLTS

TOPTICA
PRECISION

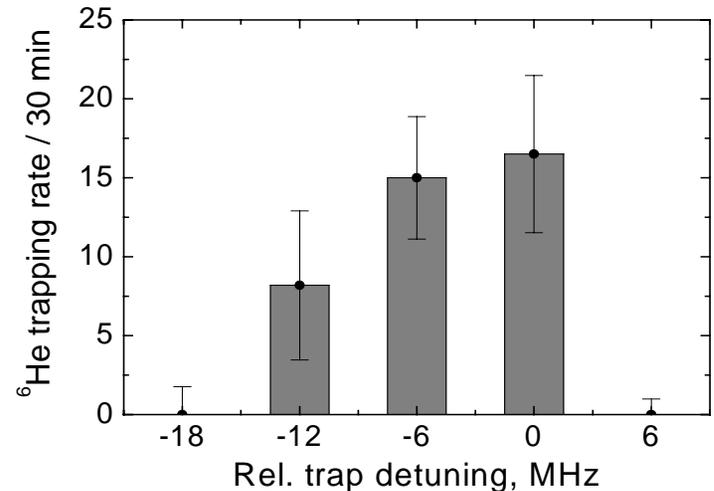
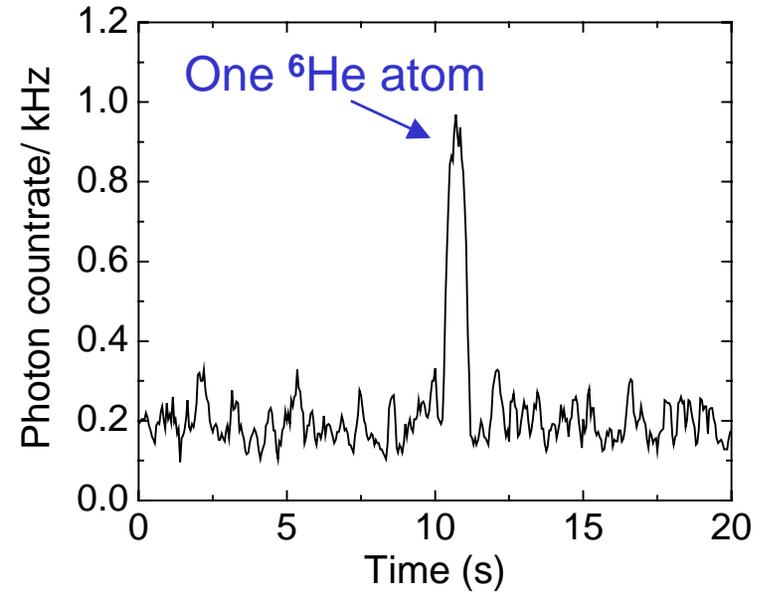


Atom Trapping of ${}^6\text{He}$



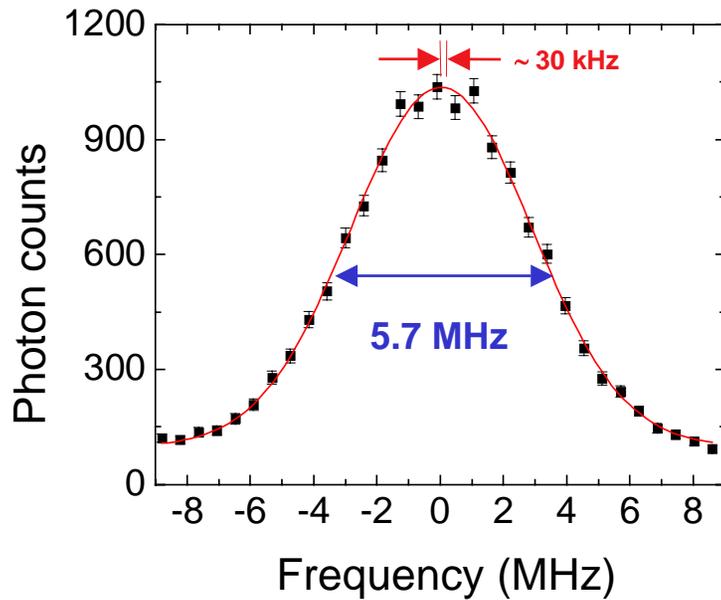
^6He - Single Atom Signal

- ❖ Capture efficiency $\sim 10^{-8}$
Single atom detection necessary!
- ❖ Single-atom signal ~ 1.0 kHz
- ❖ Single-atom S/N ~ 10 in 100 ms
- ❖ ^6He capture rate ~ 150 per hour

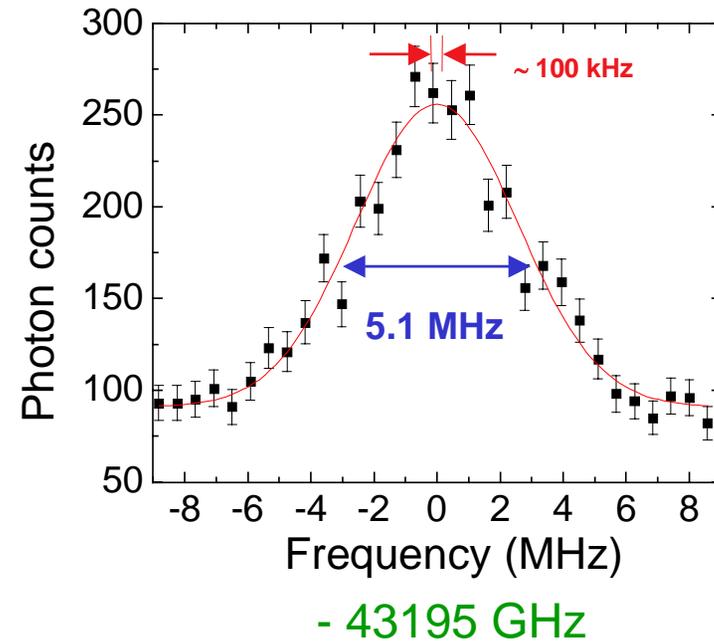


Single-Atom Spectroscopy

^4He



^6He



~ 150 ^6He atoms in one hour

Isotope Shift Result

IS ($2^3S_1 - 3^3P_2$, $^6\text{He} - ^4\text{He}$) = 43 194.772(56) MHz

RMS Charge Radius of ^6He $\langle r_c^2 \rangle^{1/2} = 2.054(14)$ fm (0.7%)

Error Budget

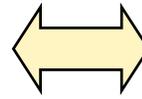
Source	Correction (kHz)	Error (kHz)
Statistical		33
Trap effects		40
Uneven background		20
Frequency counter		9
Recoil effect	+ 110	< 1
Total	+ 110	56

Recoil Correction

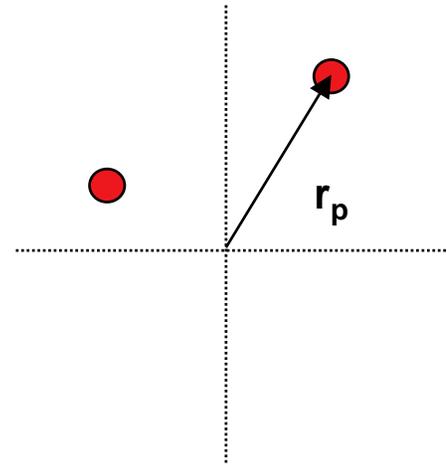
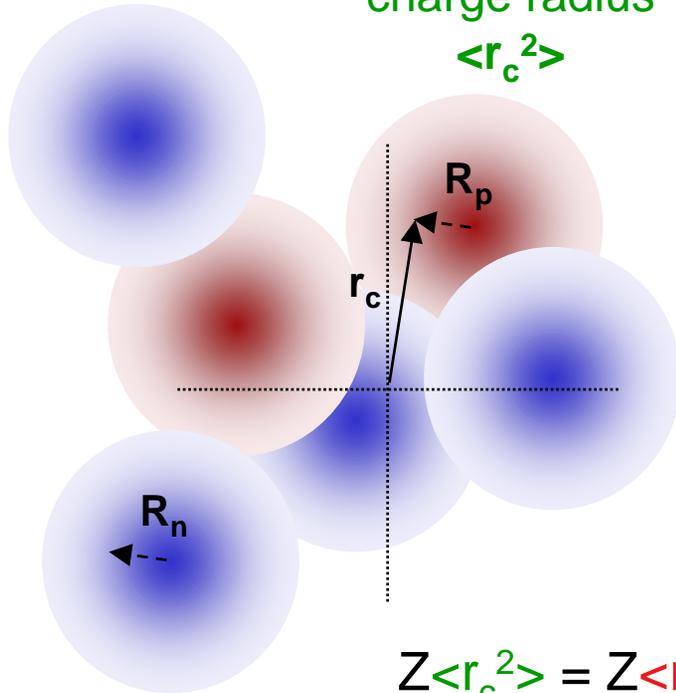
$$E_\gamma = E_{\text{int}} + \frac{P_\gamma^2}{2M_{\text{atom}}}$$

Charge Radius vs. Point-Proton Radius

Experiment:
mean square
charge radius
 $\langle r_c^2 \rangle$



Theory:
mean square
point-proton radius
 $\langle r_p^2 \rangle$



$$Z\langle r_c^2 \rangle = Z\langle r_p^2 \rangle + Z\langle R_p^2 \rangle + N\langle R_n^2 \rangle$$

Experimental mean square charge radii:

Proton $\langle R_p^2 \rangle = 0.801(32) \text{ fm}^2$

Neutron $\langle R_n^2 \rangle = -0.120(5) \text{ fm}^2$

Conclusion and Outlook

${}^6\text{He}$ Point-Proton Radius

$$\langle r_p^2 \rangle^{1/2} = 1.912(18) \text{ fm}$$

Precision

- ❖ Spectroscopy ~ 60 kHz or 0.7%
- ❖ Proton-Neutron radii $\sim 0.4\%$
- ❖ QMC theory $\sim 0.5\%$

${}^8\text{He}$ Production Rate

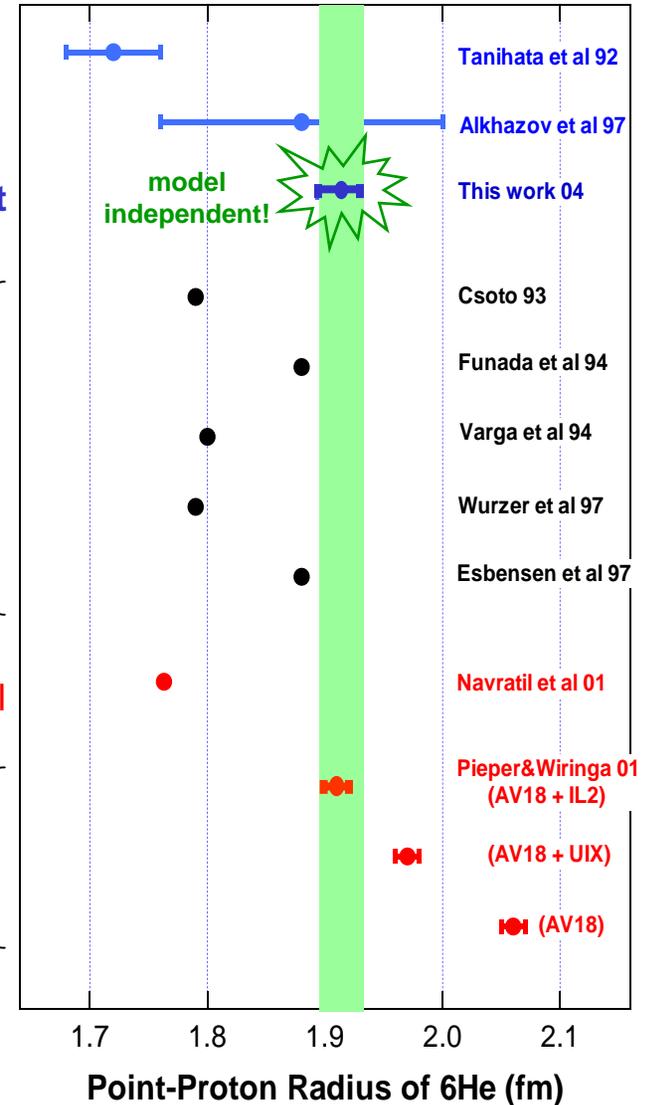
- ❖ ATLAS $\sim 10^4$ - 10^5 s $^{-1}$
- ❖ ISOLDE $>10^5$ s $^{-1}$
- ❖ NSCL $\sim 10^6$ s $^{-1}$
- ❖ RIA $\sim 10^9$ s $^{-1}$

Reaction collision
Elastic collision
Atomic isotope shift

Cluster models

No-core shell model

Quantum MC



Thank You!

Co-Authors

L.-B. Wang, K. Bailey, J.P. Greene, D. Henderson, R.J. Holt, R.V.F. Janssens, C.L. Jiang,
Z.-T. Lu, T.P. O'Connor, R.C. Pardo, K.E. Rehm, J.P. Schiffer, X.D. Tang

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Univ. of Windsor

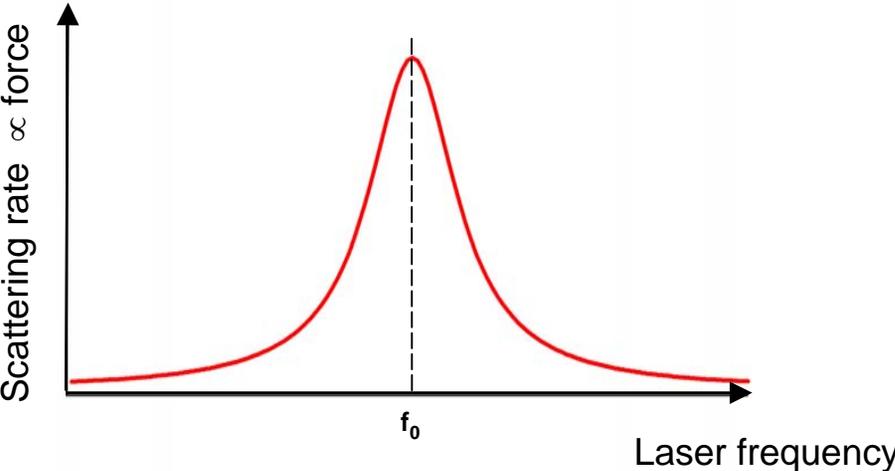
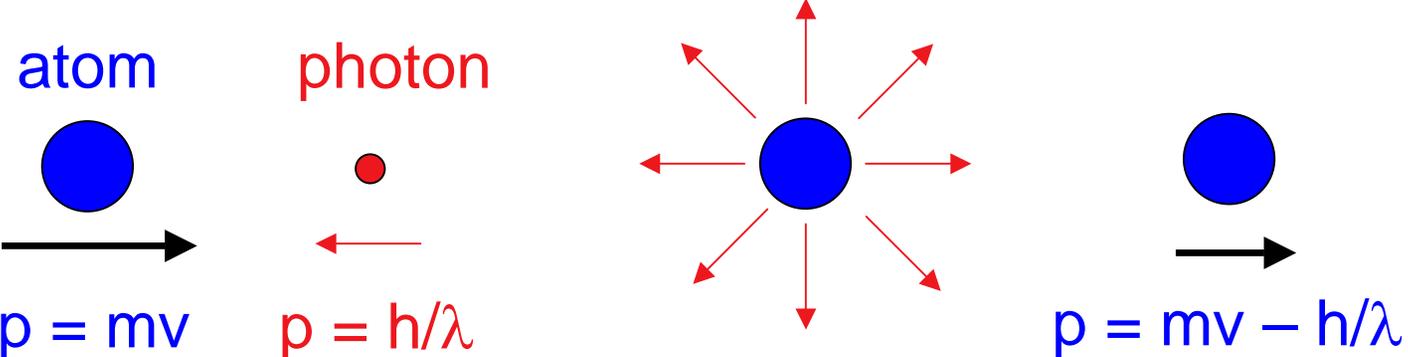
Other Collaborators

P. Collon, X. Du, A.M. Heinz, C. Law, I.D. Moore, M. Paul, T. Pennington

\$\$\$

DOE, Office of Nuclear Physics

Manipulating Neutral Atoms with Light

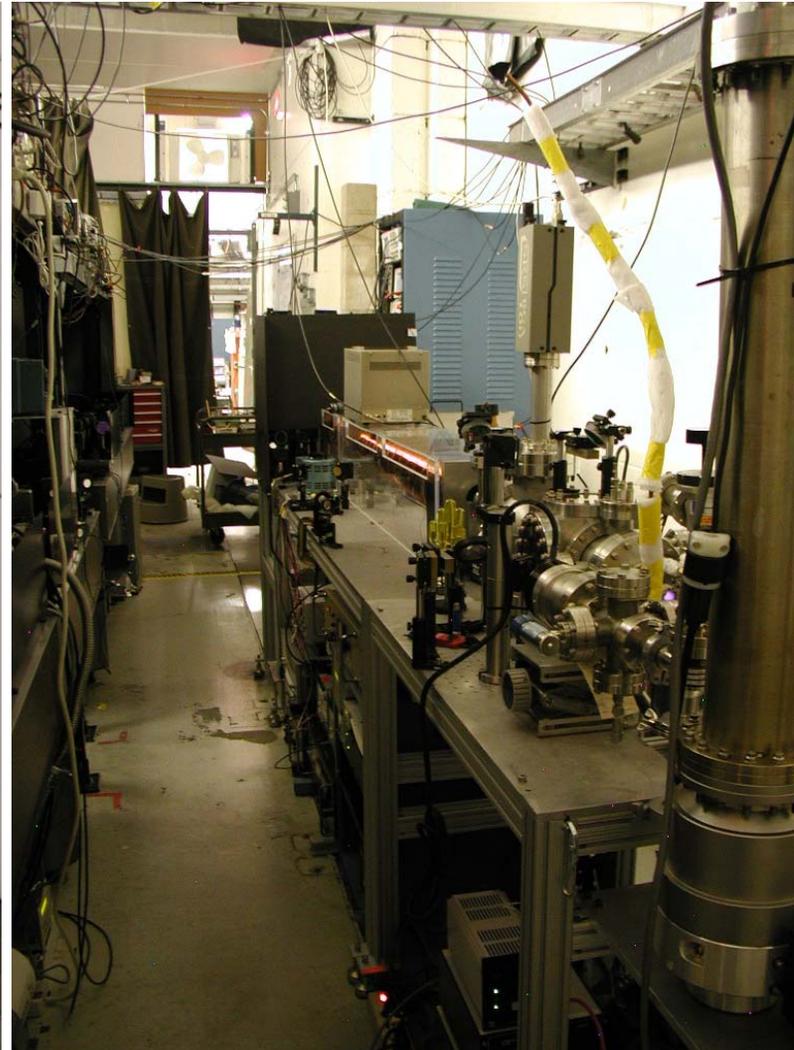
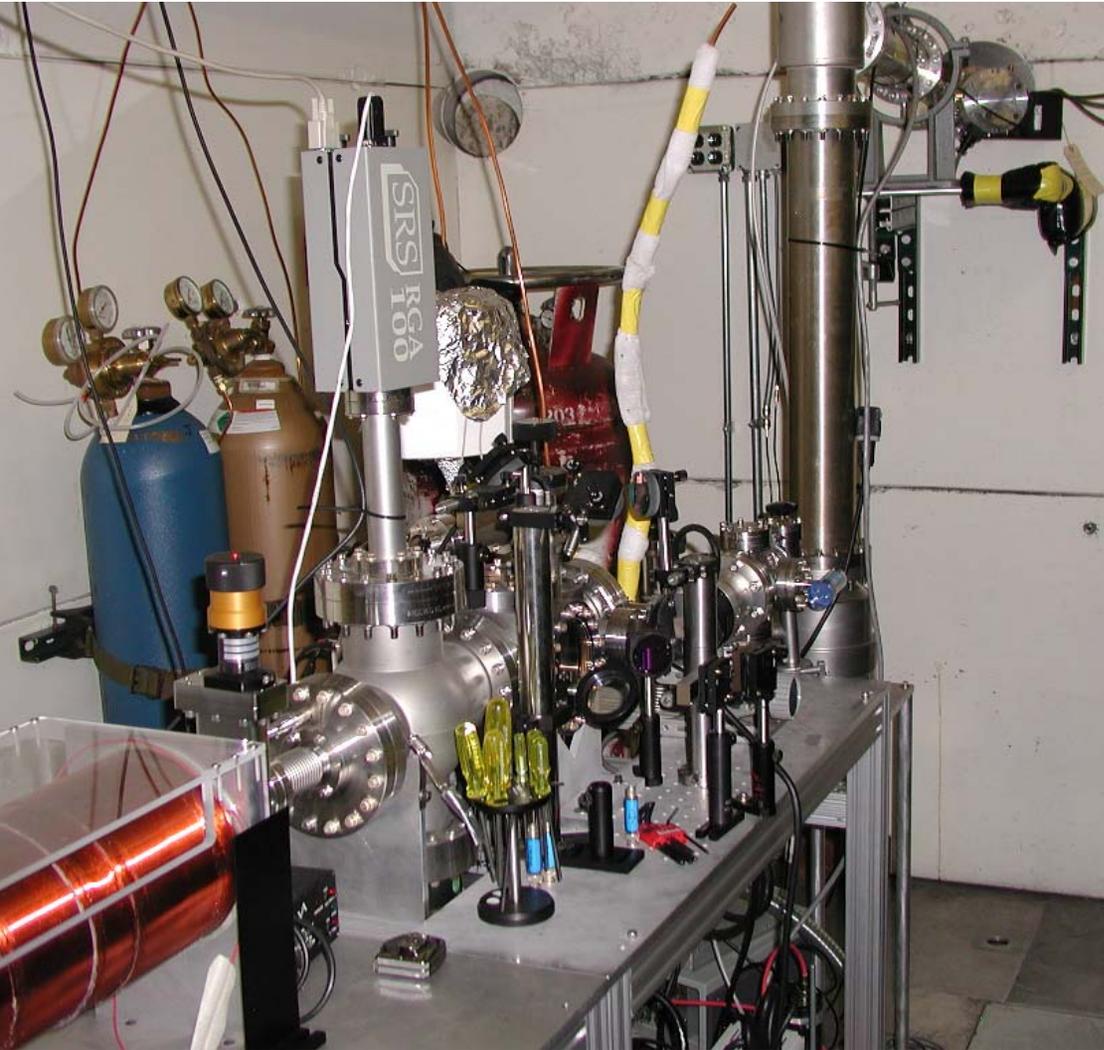


$\tau \sim 100$ ns
scattering rate ~ 5 MHz

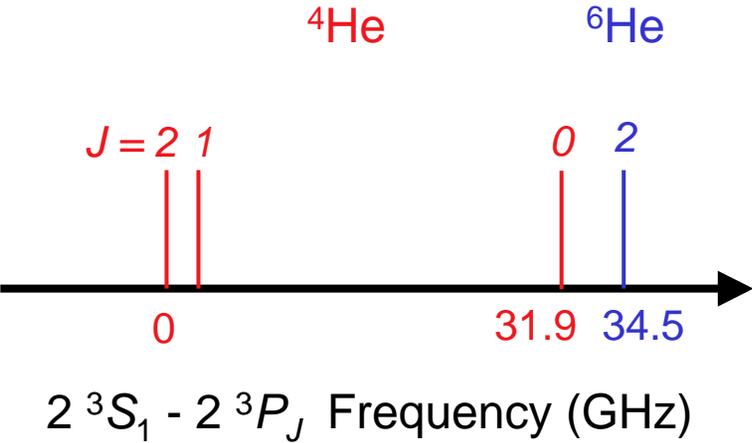
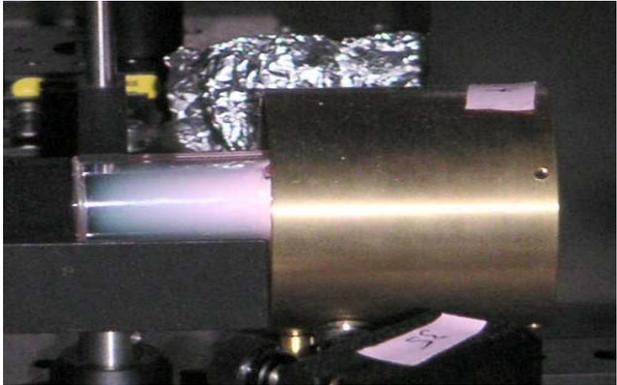
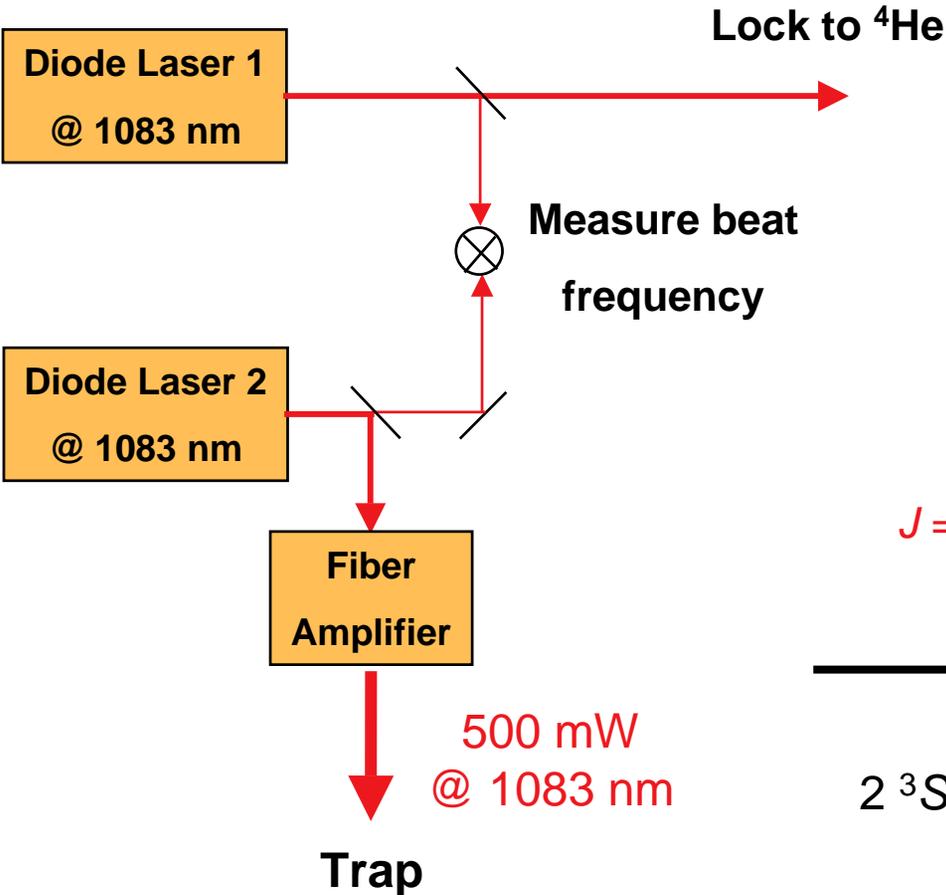
↓

$a \sim 10^4$ m/s²

Trap On-Line at ATLAS



Laser Setup - 1083 nm



Electron Scattering

- ◆ Point-charge

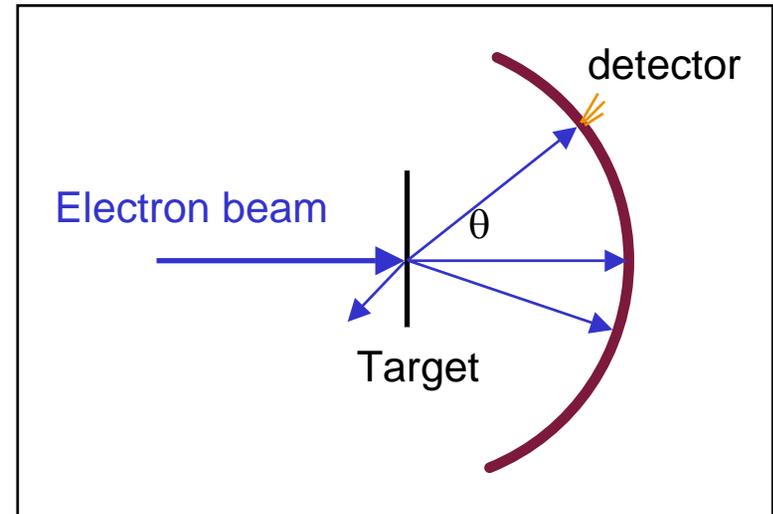
$$\left(\frac{d\sigma}{d\Omega}\right)_{Rutherford} = \frac{Z^2 \alpha^2 (\hbar c)^2}{4E^2 \sin^4 \frac{\theta}{2}}$$

- ◆ Nuclei with finite size

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{exp}} = \left(\frac{d\sigma}{d\Omega}\right)_{Rutherford} * \cos^2 \frac{\theta}{2} * |F(q^2)|^2$$

$$\langle r^2 \rangle_{\text{charge}} = -6\hbar^2 \left. \frac{dF(q^2)}{dq^2} \right|_{q^2=0}$$

- ◆ $R \sim 1.21 \times A^{1/3}$ fm for non-deformed nuclei
- ◆ **NOT** applicable to unstable (short-lived) nuclei



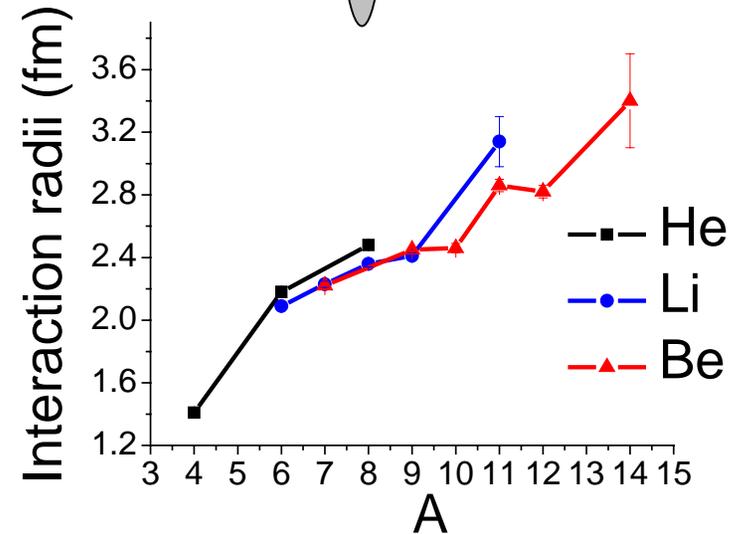
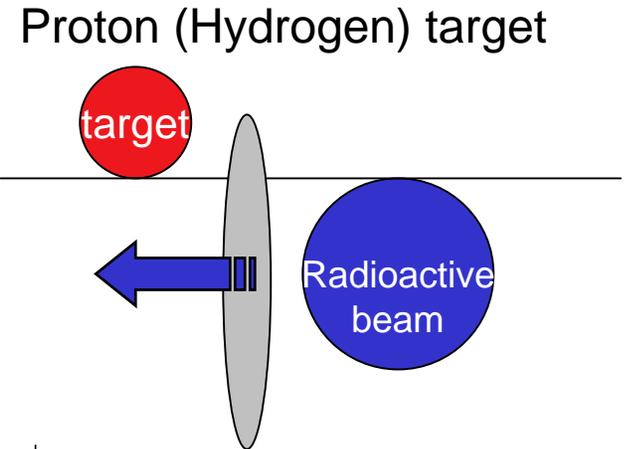
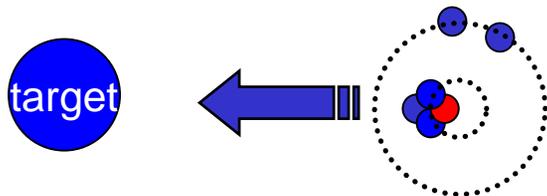
Inverse Kinematik Proton Scattering

- Interaction cross section

$$\sigma_I = \pi(R_{\text{target}} + R_{\text{beam}})^2$$
- Can not separate proton and neutron distribution model-independently
- First observation of “halo nuclei” by Tanihata, 1985

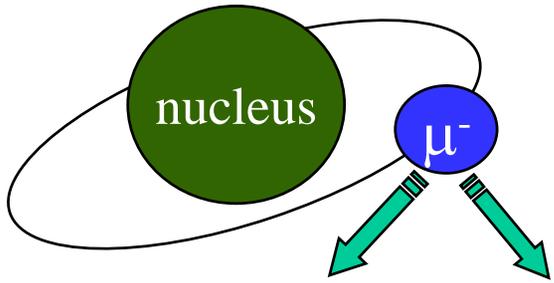
${}^6\text{He}$:

$$\sigma_I({}^6\text{He}) \sim \sigma_I({}^4\text{He}) + \sigma_{-2n}({}^6\text{He})$$



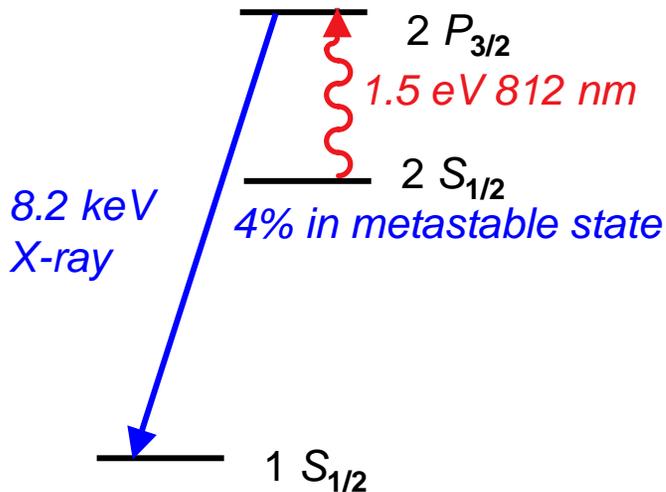
I. Tanihata, *et al.*, PRL **55**, 2676, (1985)

Muonic Atom X-Ray Spectroscopy



muon decay $\mu^- \rightarrow e^- \nu \bar{\nu}$

Muonic ${}^4\text{He}^+$ Energy Level



◆ $m_\mu/m_e \sim 200$

◆ Bohr radius

$$a_0 \sim \frac{1}{m_e}$$

◆ Energy level

$$E_n \sim -\frac{m_e}{n^2}$$

◆ Wave function

$$\Psi(r) \sim a_0^{-3/2} e^{-r/a_0}$$

◆ Energy shift due to nuclear size~

$$\Delta |\Psi(0)|^2 \langle r^2 \rangle$$

◆ Sensitivity $\sim (m_\mu/m_e)^2$

◆ $\delta\nu(2S_{1/2}-2P_{3/2}) = 1.813 - 0.102\langle r^2 \rangle$ eV

◆ $\langle r^2 \rangle^{1/2}({}^4\text{He}) = 1.673(1)$ fm,

Carboni et al., Nucl. Phys. A278, (1977)